

# A systematic literature review on the joint replenishment problem solutions: 2006–2015

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## Abstract

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Among all existing inventory replenishment models, this research was dedicated to the Joint Replenishment Problem (JRP), which consists in the replenishment of multiple items simultaneously, aiming total cost reduction. Literature has presented several optimal and approximated solutions to this problem, with different applications and techniques, which results in a large quantity of solution proposals. Therefore, this research aimed to map existing solutions to the problem in 2006–2015 in order to provide a guide for interested parts in JRP and to update previous reviews. Hence, systematic review was used to assess papers from that period interval. From a total of 128 papers, a general trend for seeking JRP extensions and practical applications was verified. Furthermore, the heuristic and metaheuristic methods were the most used and considered the most suitable due to their simplicity in understanding and application.

## Keywords

Inventory management. Multi-product. Joint replenishment problem. Systematic review.

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## 1. Introduction

For decades, more studies on inventory replenishment problems have been developed as the demand for products have increased and the cost reduction became an important objective. On a mathematical perspective, a large amount of solutions has been proposed by means of optimization models, with the objective of reducing costs and fulfilling the demand (Saracoglu et al., 2014). One of the main topics is the Joint Replenishment Problem (JRP), which consists in programming the replenishment of different types of items in the same order, generally provided by the same supplier, aiming total inventory costs reduction (Khouja & Goyal, 2008).

There is an extensive literature regarding the development of efficient and effective solution models for the JRP, that have been proposed to provide more practical models. Companies seek models to make decisions on inventory management that result in efficient JRP solutions, since the replenishment of multi-items is a common context within the operation environment (Salameh et al., 2014). Furthermore, according to Salameh et al. (2014), the JRP guarantee total cost reduction compared to single-item replenishment.

The JRP is considered NP-Hard due to its combinatorial nature. Therefore, recent studies have focused on finding more efficient and faster solution algorithms, also considering the practical context in where the problem is presented, such as metaheuristic methods, instead of only generating exact solutions, as it results in large computational time (Khouja & Goyal, 2008; Qu et al., 2015). Porras & Dekker (2008) assert that the joint replenishment strategy results in saving up to 13% on the total cost compared to Economic Order Quantity models for a single item approach considering a set of twenty products.

The practical application of JRP models can be difficult as its complexity may easily increase computational time. The available published literature provides a large variety of models and applications, with different methods, that seek lower computational time, optimal solutions, or, in their minority solving practical approaches. Furthermore, there has been a time gap since the last review about JRP models provided in Khouja & Goyal (2008), and the update of the state of art on JRP may help researchers and professionals on knowing the latest approaches.

Therefore, this study aimed to map the different existing solution methods for the JRP, by means of Systematic Review, considering the knowledge developed between 2006 and 2015. This range was chosen as an extension to the work developed in Khouja & Goyal (2008), which performed a review of methods within 1989-2005. Hence, a Systematic Review Protocol was created to guide the review and provide references for those who are interested in the JRP.

In addition to this introduction, this paper presents the concepts regarding the JRP, its terminology and characteristics, as well as the main contributions stated in the literature on Section 2. Then, on Section 3, the systematic research guidelines and the research protocol are presented. The results on Section 4 are shown in categories regarding demand behavior, which were discussed in terms of planning horizon, solution methodology, and main results. Finally, Section 5 presents the conclusion, followed by the References section.

## 2. The joint replenishment problem in inventory management

The JRP occurs when one considers the interdependency among different groups of products in a same order provided by a single supplier, in the inventory replenishment process (Khouja & Goyal, 2008; Wang et al., 2012b; Salameh et al., 2014). The objective is to optimize the total replenishment cost by reducing the inventory ordering and holding costs (Wang et al., 2012c; Salameh et al., 2014; Qu et al., 2015; Wang et al., 2015). Hence, the joint replenishment presents two advantages: it is possible to earn discounts from the supplier when ordering large batches of multiple items; and the (ordering) fixed costs per item can be reduced as well as the transportation costs (Salameh et al., 2014).

JRP models have presented a large diversity of application. As the problem is considered NP-Hard, it is more difficult to find solutions in acceptable computational time, and that are practical for the decision-making process in companies compared to single-item inventory replenishment models (Khouja & Goyal, 2008; Wang et al., 2012c). In the literature, models consider two main solving strategies for the JRP (Khouja & Goyal, 2008): Direct Grouping Strategy (DGS) - products are grouped in sets, in which each group the items follow the same cycle time; and Indirect Grouping Strategy (IGS) - each product has its own cycle time, that is a multiple of a basic cycle time (Wang et al., 2015).

Also, two types of ordering costs are considered: the major ordering cost and minor ordering cost. The former is related to the ordering cost of the whole batch and the latter is associated with each item that composes the order to be replenished (Zhang et al., 2013). In the IGS, for instance, the total cost ( $TC$ ) is defined as the sum of total holding cost and the total ordering cost, which is composed by the sum of total minor ( $s_i$ ) and major ( $S$ ) ordering costs, as stated in the Equation 1.  $\mathbf{K}$  is the vector of  $k_i$ , that corresponds to the integer multipliers of the basic cycle time  $T$  for each product  $i$ , and  $h_i$  is the holding cost of each product from the total  $n$  products.

$$TC(T, \mathbf{K}) = HC + OC = \frac{T}{2} \sum_{i=1}^n k_i D_i h_i + \frac{\left( S + \sum_{i=1}^n \frac{s_i}{k_i} \right)}{T} \quad (1)$$

By means of experiments in simulation, it was observed that the IGS was more efficient than the DGS when the ratio major/minor ordering costs was high, and the DGS presented better results mostly in computational time when the ratio was lower (Olsen, 2005; Porras & Dekker, 2006; Khouja & Goyal, 2008).

Some of the main JRP solution methods and contributions presented by Khouja & Goyal (2008) are seen in Table 1. On deterministic models, the main reference is the RAND algorithm, proposed by Kaspi & Rosenblatt (1991). It is a heuristic that divides equally a range of cycle time values among lower and upper bounds and then it applies Silver (1976)'s algorithm (Khouja & Goyal, 2008). At the time, RAND was considered the best algorithm due to its satisfactory results for instances with a large product quantity in terms of solution quality and computational time. Furthermore, it can be easily implemented compared to other algorithms, which made it one of the main methods for comparison and validation of newer models (Khouja & Goyal, 2008).

On the stochastic demand models, there are two main replenishment policies: The can-order policy (COP), by Balintfy (1964), in which if any item reaches a must-order point, a replenishment order is made, and if the

**Table 1.** Main solution models for the JRP until 2006.

Demand	Solution approaches	Related Works
Deterministic (non-time varying)	Enumerative Algorithms and Branch-and-Bound, Global Optimization Algorithms, RAND, Heuristics and Genetic Algorithms.	Goyal & Deshmukh (1993); van Eijs (1993); Viswanathan (1996, 2002); Hariga (1994); Wildeman et al. (1997); Fung & Ma (2001); Olsen (2005); Porras & Dekker (2006)
Dynamic (time varying)	Branch-and-bound, Dantzi-Wolf decomposition, Power-of-Two technique and Heuristics, Dynamic Programming	Silver (1979); Lee & Yao (2003); Boctor et al. (2004)
Stochastic	Can-order policy and Periodic Replenishment Policy variants; Poisson or Normal distribution on demand; Policy Parameters estimation; Markov Decision Process.	Silver (1981); Pantumsinchai (1992); Johansen & Melchior (2003); Nielsen & Larsen (2005); Lee & Chew (2005); Minner & Silver (2005); Özkaya et al. (2006)

Source: Khouja & Goyal (2008).

other items present inventory levels below a can-order point, they are included in the same order (Johansen & Melchior, 2003; Balintfy, 1964; Khouja & Goyal, 2008). The periodic replenishment policy (PRP), by Atkins & Iyogun (1988), or (T, M) policy, considers a Poisson distributed demand, in which all products follow the same replenishment periodic interval T, and each one is replaced to a pre-determined inventory level M. Later, it has been considered that a set of products would follow the periodic review interval T, while other products that also should be replenished would follow a section of T (Atkins & Iyogun, 1988; Khouja & Goyal, 2008).

More sophisticated methods were also used to solve the JRP, such as meta-heuristics, Evolutionary Computing, Genetic Algorithms, and Differential Evolution Algorithm (Wang et al., 2015). Moreover, Khouja & Goyal (2008) stated that the focus on finding the optimal solution has been saturated and suggested efforts to be directed on the development of more practical models which can be implemented easily in companies. Further details are shown in Khouja & Goyal (2008).

### 2.1. Systematic review

It comprehends a rigorous process that allows transparency on the steps followed by the research, by means of protocols, to identify, assess and summarize the main contributions on literature regarding a defined topic, diminishing bias and highlighting the review steps of the researcher (Tranfield et al., 2003; Thomé et al., 2016). Therefore, based on previous guidelines, Thomé et al. (2016) presented the following general steps, which may lead researchers while performing a systematic review: Problem Formulation and Review Planning, Literature Search, Data Collection, Data Analysis, Data Synthesis and Interpretation, Results Presentation and Review Update.

### 3. Research methodology

For achieving the objective of mapping the different existing solutions on JRP, this research performed a Systematic Review considering published material in the range 2006–2015. Hence, this study followed the guidelines provided in Tranfield et al. (2003) and Thomé et al. (2016), being the first step the creation of the research question and the Review Protocol.

For this purpose, the question that guided the procedure of the systematic review was defined: “What is the context of JRP inventory studies, published in the period of 2006 to 2015, with respect to the method, context and main results of the solutions?”.

After an initial literature review on JRP, the key-words to search papers were obtained. The inclusion criteria comprised of accepting articles that proposed new, revised or improved models on JRP. As exclusion criteria, papers with only single-item replenishment approaches were not considered as they are not JRP.

Therefore, the collection of articles followed the Review Protocol, as shown in Table 2, and they were chosen by analyzing their titles, abstract and keywords, as well as in completely accordance among the authors for acceptance. The use of five electronic databases allowed a fast and broader search for the desired material.

From selected papers, information regarding assumptions of the model and its application was extracted, such as: the solution development method or modelling, the context in which the JRP was presented and the method was applied, as well as the main results obtained, in terms of solution quality (deviation from the best known solutions) and computational time.

The models were categorized by the type of demand (deterministic or stochastic) and information regarding inventory management theory was also obtained, as in Khouja & Goyal (2008). In addition, complementary approaches in where the JRP is presented indirectly as within a general problem or related to other problems were also considered.

Table 2. JRP Systematic Review Protocol.

Research question: “What is the context of JRP inventory studies, published in the period of 2006 to 2015, with respect to the method, context and main results of the solutions?”			
Key-words	Range	Inclusion criteria	Databases
Joint Replenishment Problem	2006-2015	Journal Papers Proposal of models for the JRP - Development and application of new models or improvements on previous methods.	Web of Science PROQUEST
Joint Replenishment Model		Comparisons on JRP models, JRP and single-item models, literature reviews.	SCOPUS
Multiple Inventory Replenishment		Exclusion criteria Approaches only on single-item replenishment	CAPES Journals Google Scholar

#### 4. Analysis of results

A total of 128 papers were obtained, which demonstrates a considerable amount of contributions to the topic. As shown in Figure 1, the JRP has been widely studied and its importance implies in continuous research efforts. In addition, the increase in quantity can be justified by the development of faster computation algorithms contributing to the solving of NP-Hard problems as the JRP.

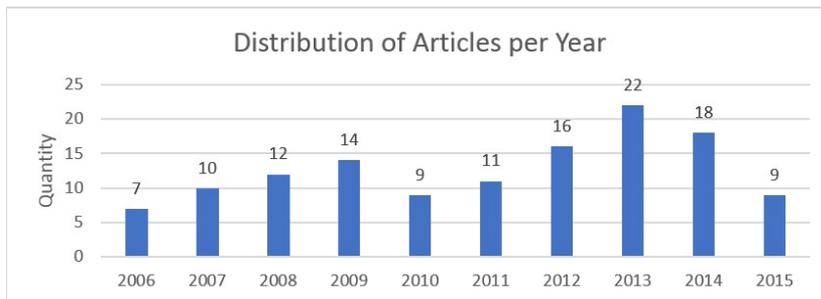


Figure 1. Distribution of Published articles per year from the databases.

As shown in Table 3, the International Journal of Production Economics and the European Journal of Operational Research are those containing most of the selected papers with 18 and 16 articles, respectively. One can verify the JRP is an ongoing topic, which encourages the new studies to extend the application of the multi-item replenishment context, especially due to its advantages in inventory management decisions.

Table 3. Ranking of 10 most frequently publication journals.

Repository	Articles
International Journal of Production Economics	18
European Journal of Operational Research	16
Computers & Operations Research	7
International Journal of Production Research	6
Computer Integrated Manufacturing Systems	6
Operations Research	6
Expert Systems with Applications	5
International Journal of Systems Science	4
The International Journal of Advanced Manufacturing Technology	4
Transportation Research Part E: Logistics and Transportation Review	4

In addition, as verified in Table 4, there has been a predominance of models on the Deterministic Demand category (constant and dynamic), even though it had always presented a solid study, followed by the Stochastic Demand models. It can also be noticed a high quantity of articles on complementary approaches of the JRP, which states a broader extension of JRP in the literature

Table 4. Quantity of Articles per category of demand.

Type of Demand	Quantity
Constant Deterministic	36
Dynamic Deterministic (time-varying)	2
Stochastic	19
Complementary Approaches	71

The presence of practical applications of the JRP, with a focus on daily problems on companies also confirms that the models aimed obtaining good solutions for cost reduction and not only the optimal cost solution, as suggested by (Khouja & Goyal, 2008).

#### 4.1. Deterministic and dynamic demand

On constant deterministic demand models, it was observed that the infinite horizon planning approach comprehended most papers (80%), representing a generalization of the JRP application. As shown in Table 5, 24 papers developed heuristic or meta-heuristic methods, which provided easy implementation, using intuitive algorithms on less complex platforms, such as spreadsheets as in Nilsson et al. (2007). Therefore, the JRP has been widely applied to practical problems, and papers showed solutions on lower computational times, compared to exact solutions, what supports Khouja & Goyal (2008) suggestion for future works.

Table 5. Models on Constant and Dynamic Deterministic Demand.

Author (Year)	Method
Porras & Dekker (2006) <sup>1</sup> , Hoque (2006) <sup>1</sup> , Bayindir et al. (2006) <sup>1</sup> , Zhang et al. (2011) <sup>1</sup> , Zhang (2012) <sup>1</sup>	Global Optimization Algorithms <sup>(c)</sup>
Levi et al. (2006) <sup>2</sup>	Mixed Integer Programming <sup>(c)</sup>
Nilsson et al. (2007) <sup>1</sup> , Amaya et al. (2013) <sup>1</sup> , Zhang et al. (2012) <sup>1</sup> , Tsao & Teng (2013) <sup>1</sup> , Paul et al. (2014) <sup>1</sup> , Bayley & Bookbinder (2015) <sup>1</sup> , Praharsi et al. (2010) <sup>1</sup> , Gutiérrez et al. (2013) <sup>1</sup>	Heuristics <sup>(a)</sup>
Ho (2013) <sup>1</sup> , Salameh et al. (2014) <sup>1</sup>	Heuristics <sup>(c)</sup>
Moon & Cha (2006) <sup>1</sup>	Genetic Algorithm and RAND with Lagrange Multipliers <sup>(a)</sup>
Yoo & Gen (2007) <sup>1</sup>	Genetic Algorithm and Simulated Annealing <sup>(a)</sup>
Liang et al. (2009) <sup>1</sup>	Simulated Annealing and Lagrange Relaxation <sup>(a)</sup>
Wang & Cheng (2008) <sup>1</sup>	RAND <sup>(c)</sup>
Porras & Dekker (2008) <sup>1</sup>	Enumerative Algorithm <sup>(a)</sup>
Taleizadeh et al. (2008) <sup>1</sup>	Harmony Search Algorithm <sup>(a)</sup>
Olsen (2008) <sup>1</sup> , Li et al. (2015) <sup>1</sup>	Evolutionary Algorithm <sup>(a)</sup>
Hong & Kim (2009) <sup>1</sup> , Taleizadeh et al. (2013) <sup>1</sup>	Genetic Algorithm <sup>(a)</sup>
Hsiau & Lin (2009) <sup>1</sup>	Simulated Annealing <sup>(a)</sup>
Taleizadeh et al. (2009) <sup>1</sup>	Meta-heuristic and Fuzzy Rough Algorithm <sup>(a)</sup>
Taleizadeh et al. (2011) <sup>1</sup>	Harmony Search, Rough Simulation and Fuzzy Simulation Algorithms (Hybrid) <sup>(a)</sup>
Wang et al. (2012b) <sup>2</sup> , Wang et al. (2012c) <sup>1</sup>	DEA <sup>(a)</sup>
Moon et al. (2011) <sup>1</sup>	RAND with Heuristics <sup>(a)</sup>
Kang et al (2013) <sup>2</sup>	Mixed Integer Programming and Particle Swarm Optimization (Hybrid) <sup>(c)(a)</sup>
Durán & Pozo (2013) <sup>1</sup>	Particle Swarm Optimization and Genetic Algorithm <sup>(a)</sup>
Yousefi & Sadjadi (2014) <sup>1</sup>	RAND and Genetic Algorithm (Hybrid) <sup>(a)</sup>
Wee et al. (2009) <sup>2</sup>	Fuzzy Model & Multi-Objective <sup>(a)</sup>

<sup>1</sup>Finite Planning Horizon; <sup>2</sup>Infinite Planning Horizon; <sup>(c)</sup>Exact Solution; <sup>(a)</sup>Approximated Solution.

One of those approaches was the use of cost balancing for approximating a certain solution to the optimal, such as of a ratio between ordering costs and holding costs, and, thus, consisted on a fast decision mean of scheduling orders (Nilsson et al., 2007). Also, the authors justified the use of hybrid algorithms due to the potential complementarity different methods can present for achieving better quality solutions. In addition, one can verify the use of the Differential Evolution Algorithm (DEA), by Wang et al. (2012b, c). While most of the models were based on the IGS, the use of DEA considered the DGS due to a relatively lower computational time for solving the problem.

Furthermore, there has been a trend in solving practical problems by considering additional situations such as capacity and resource constraints, in Hoque (2006); Porras & Dekker (2006), Wang & Cheng (2008), Amaya et al. (2013), Li et al. (2015). Studies of Zhang et al. (2011, 2012) and Zhang (2012) presented the replenishment of a main individual item and its complementary products whose demand is correlated to the former. Other situations considered deterioration factors of products, as in Wee et al. (2009) and Taleizadeh et al. (2013); the incorporation of errors in demand prediction, in Wang & Cheng (2008); and the presence of a utilization factor for each product as they have been replenished, on Bayindir et al. (2006).

Heuristic models have achieved high quality solutions, which were close to the optimal results they have been compared with in each article. The deviation value from optimal solutions in some models were in average 0.07% higher in terms of total costs, as in Zhang et al. (2012).

Moreover, there was a small quantity of models performed that comprised the dynamic demand environment, which were Gutiérrez et al. (2013) and Praharsi et al. (2010). Differently from the usual deterministic models, there is not a constant ratio of demand over time, although it is known in advance. Hence, it varies on discrete time intervals, which increases the complexity of problems, especially due to the difficulty in modelling the problem in the analytical form.

Simultaneously, this situation fits the reality of some companies, when replenishment contracts are made. In this case, companies must establish the correct cycle time for each replenishment to avoid stock-out. Hence, it was verified a large opportunity of researching considering this approach within the deterministic demand models.

## 4.2. Stochastic demand

On stochastic demand models, there was a large quantity of proposals on inventory replenishment policies based on the COP and as it comprises of a continuous review policy, it presented a potential to decrease the quantity of safety inventory in case of a correct estimation of re-order and can-order parameters. The solution methods have focused mostly on determining the optimal values for those parameters and proposed the best suitable values for the can-order policies, as shown in Table 6. Therefore, a total of three papers used a Markov Decision Process approach, as in Minner & Silver (2007), Kayış et al. (2008), and Feng et al. (2015). In this case, the demand was considered as a compound Poisson distribution for each type of product to be replenished in the same order. In addition, decomposition methods were also present, in which the JRP was decomposed in several single-item problems one for each type of product, as in Huang & Chen (2007), Kayış et al. (2008), and Larsen (2009), and the solution comprehended the merge of each sub-solution obtained.

Table 6. Models on Stochastic Demand.

Author (Year)	Method
Larsen (2009) <sup>1</sup>	Global Optimization Algorithms <sup>(c)</sup>
Huang & Chen (2007) <sup>1</sup> , Eynan & Kropp (2007) <sup>1</sup> , Moon et al. (2008) <sup>1,2</sup> , Yao (2010) <sup>1</sup> , Narayanan & Robinson (2010) <sup>2</sup> , Roushdy et al. (2011) <sup>1</sup> , Karalli & Flowers (2011) <sup>1</sup>	Heuristics <sup>(a)</sup>
Li et al. (2009) <sup>1</sup> , Nagasawa et al. (2015) <sup>1</sup>	Genetic Algorithm <sup>(a)</sup>
Minner & Silver (2007) <sup>1</sup>	Markov Decision Process and Heuristics <sup>(a)</sup>
Feng et al. (2015) <sup>1</sup>	Markov Decision Process and Heuristics <sup>(a)</sup>
Kayış et al. (2008) <sup>1</sup>	Markov Decision Process, Heuristics and Enumerative Algorithm <sup>(a)</sup>
Tsai et al. (2009) <sup>1</sup>	Association Clustering Algorithm <sup>(a)</sup>
Kiesmüller (2010) <sup>1</sup>	Heuristics <sup>(a)</sup>
Hernández et al. (2012) <sup>1</sup>	Golden-Section Algorithm <sup>(a)</sup>
Wang et al. (2013a) <sup>1</sup>	Fuzzy Model and Meta-Heuristics (Hybrid) <sup>(a)</sup>
Buchbinder et al. (2013) <sup>1</sup>	Primal-Dual Algorithm <sup>(a)</sup>
Wang et al. (2015) <sup>1</sup>	Meta-heuristics <sup>(a)</sup>

<sup>1</sup>Finite Planning Horizon; <sup>2</sup>Infinite Planning Horizon; <sup>(c)</sup>Exact Solution; <sup>(a)</sup>Approximated Solution.

Studies regarding stochastic demands have presented a higher complexity to the JRP, due to the uncertainty parameters, although they approximate real situations. However, a few papers good results in terms of cost, as in the analysis of Eynan & Kropp (2007) and Kayış et al. (2008), including more efficiency than Pantumsinchai (1992). On comparisons with RAND, some proposed models were lower or approximated in performance, which highlights the importance of the former for solving JRP, even in the stochastic environment (Hernández et al., 2012).

### 4.3. Complementary approaches

In this category, the first main indirect application of the JRP was presented in the Multi-echelon problems, which considered stage models covering three stages on a supply chain, mostly suppliers, manufacturer and retailer, as it is shown in Table 7. The next applications are also considered as particular situations of the multi-echelon context as they connect two different supply chain stages. The three main approaches comprehend a total of 40 papers.

Table 7. Main problems and related works on complementary approaches for the JRP.

Context	Related works
Multi-echelon	Özkaya et al. (2006), Pourakbar et al. (2007), Jung & Mathur (2007), Chen & Chen (2007), Qinglong et al. (2008), Nonner & Souza (2009), Hsu (2009), Tsao (2010), Hajji et al. (2011), Tsao & Sheen (2012), Zhou et al. (2013), Wang et al. (2013b), Ben-Daya et al. (2013), Sana et al. (2014), Büyükkaramikli et al. (2013), Coelho & Laporte (2014), Wang et al. (2014), Cordeau et al. (2015)
SWMR	Anily & Haviv (2007), Cha et al. (2008), Zhang (2009), Minner (2009), Abdul-Jalbar et al. (2010), Solyald et al. (2010), Fiestras-Janeiro et al. (2011), Elomri et al. (2012), Yang et al. (2012), Dror et al. (2012), Larsen & Turkensteen (2014), Yi & Reklaitis (2014), Praharsi et al. (2014), Ho et al. (2014), Verma et al. (2014), Pukcarnon et al. (2014)
JRD	Huang & Lin (2010), Wang et al. (2012a), Qu et al. (2013), Wang et al. (2013c), Cui et al. (2014), Zeng et al. (2014), Nagarajan & Shi (2015)

In second, there were models on the Single Warehouse Multi-retailer problem (SWMR), in which a warehouse must manage the replenishments from suppliers to a set of retailers, finding the optimal configuration of the system (Yang et al., 2012), as well as the Joint Replenishment & Delivery Problem (JRD), which approaches the delivery scheduling (routing) of multi-products along with the joint replenishment problem (Pukcarnon et al., 2014).

Other less frequent approaches involved very specific problems, which presented a diversity of models for solving multi-product related problems, especially considering practical application in companies. Therefore, the inclusion of the JRP in other problems is able to state the importance of including the multi-product environment on solving models regarding inventory replenishment, and have the potential of being the basis for the development of new specific and practical studies.

### 5. Conclusion

This study performed a literature review on the existing solutions for the JRP published between 2006 and 2015, and resulted in an information base about the main models, updating the review of Khouja & Goyal (2008), with a total of 139 selected papers. Most of them still have presented applications to constant and dynamic deterministic demands. However, the studies regarding the stochastic demand are also increasing as they approximate to practical situations. The research question was answered and the objective was achieved.

For all demand categories, authors could highlight which meta-heuristics were most used. One of the reasons was their simplicity in implementation and understanding, and presented lower computational time compared to exact algorithms, with good quality solutions. Also, for situations in where the planning horizon is large (years), a high computational time could be accepted, since the model would be used less frequently.

Furthermore, indirect approaches on the JRP were also verified, in which it was used in other problems from more general situations. In this case, there has been an extension of the problem, that considered applications for multi-echelon (three-stage replenishment), as well as related to the Single-Warehouse and Multi-Retailer problems. Hence, there has been a trend on models for simplifying the application and implementation of solution methods resulting in lower computational time as well.

Therefore, for future works, it is suggested for this review to be updated periodically to offer an up-to-date repository of models that can be used for academic or professionals interested in the JRP. Furthermore, the new development of models on dynamic demand and stochastic demand due to the opportunity of research on the form and the high complexity of the latter, which can present challenges for developing more efficient methods, and, hence, encourage the studying on the JRP.

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